

Enhancing model based acoustic localisation using quantum annealing

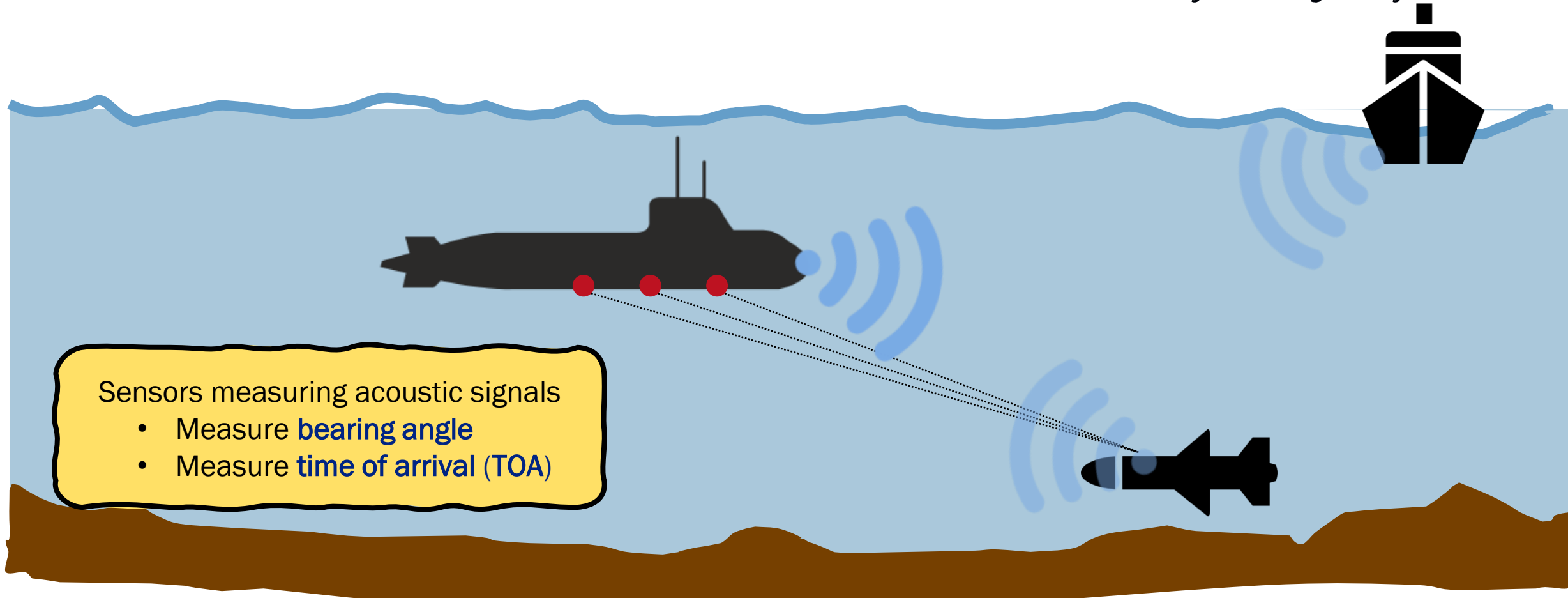
R.S. Wezeman MSc | Tariq Bontekoe MSc |
Dr. Sander von Benda-Beckmann|
Prof. dr. Frank Phillipson



Underwater target localisation

Acoustic localisation is the use of sound to **determine the distance and direction** of its source or reflector.

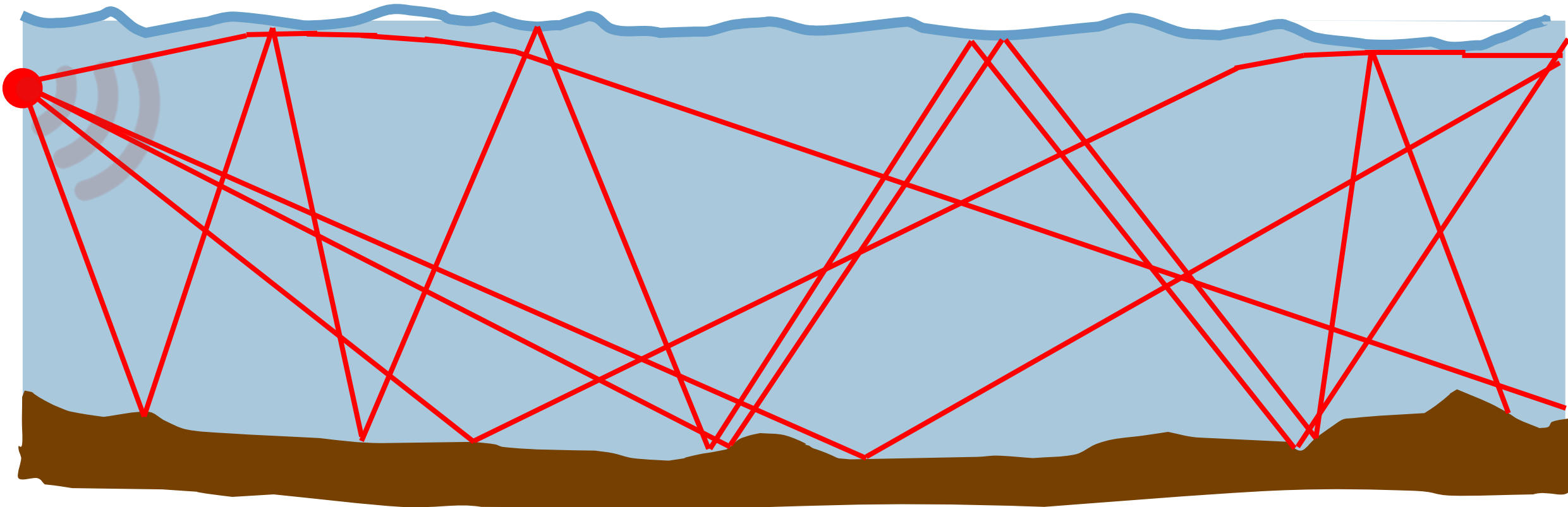
- **Passive acoustic localisation:** Involves detection of sound/vibration created by the target object.



Acoustic underwater propagation

Assumption of linear propagation of acoustic waves is not true underwater.

- **Reflections** through the ocean's bottom or ocean's surface result in loss of intensity
- **Variable sound speed.** The speed of acoustic waves depends on many parameters such as: *temperature, pressure (depth) and salinity*

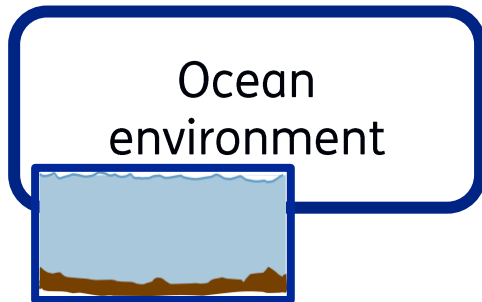


Model-based acoustic localisation

*A typical way to solve an acoustic localisation problem is by using a **model-based approach**.*

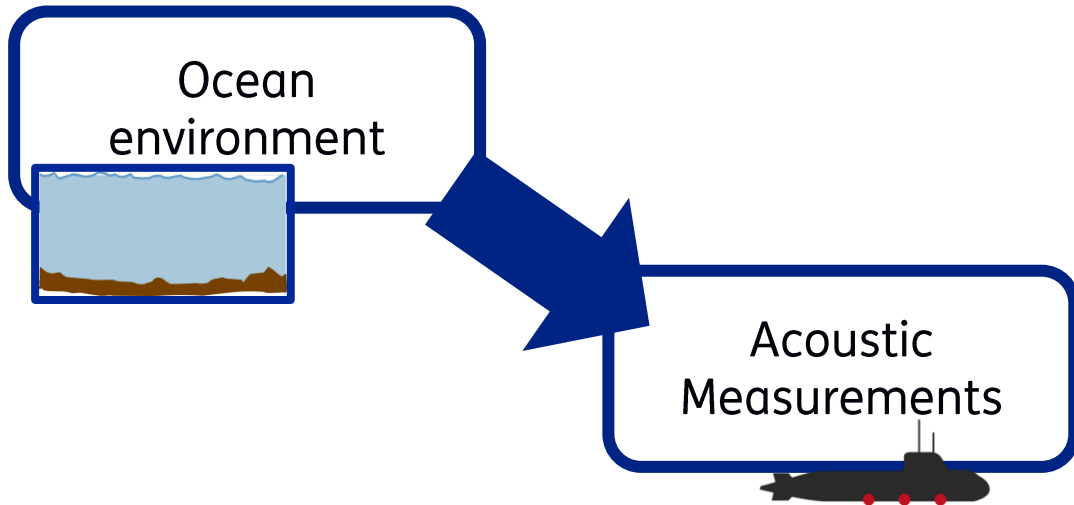
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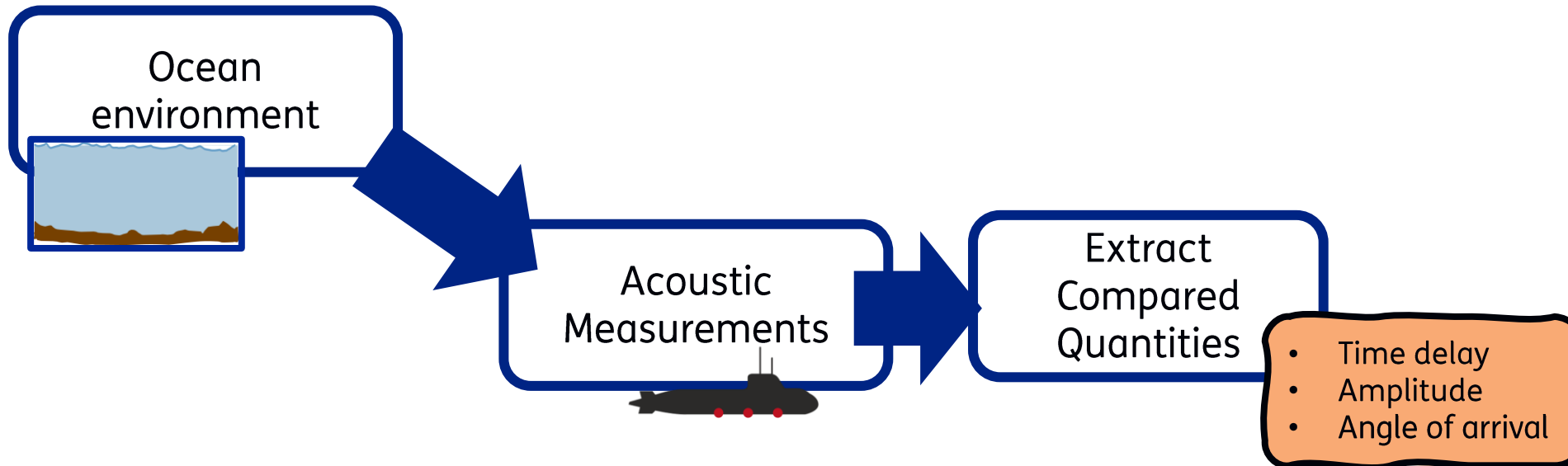
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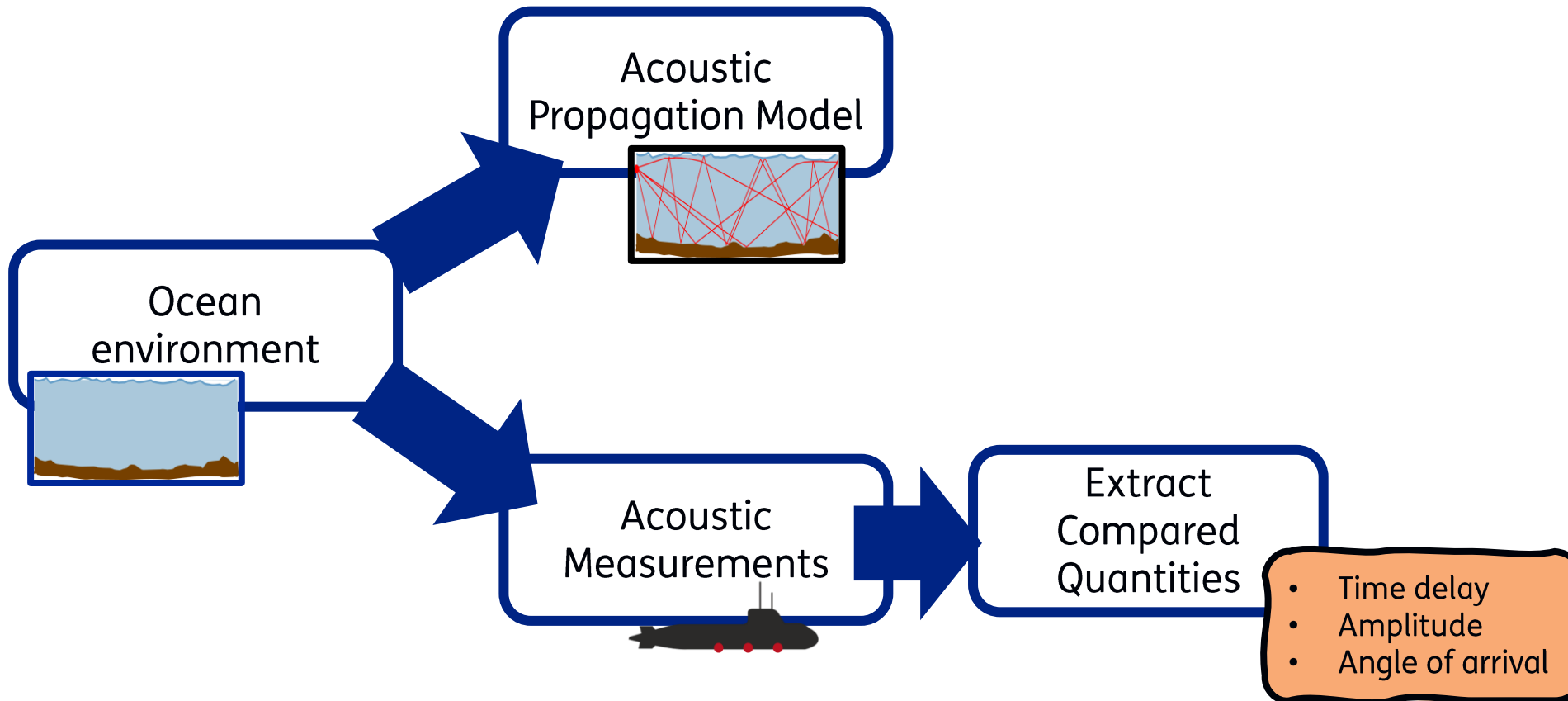
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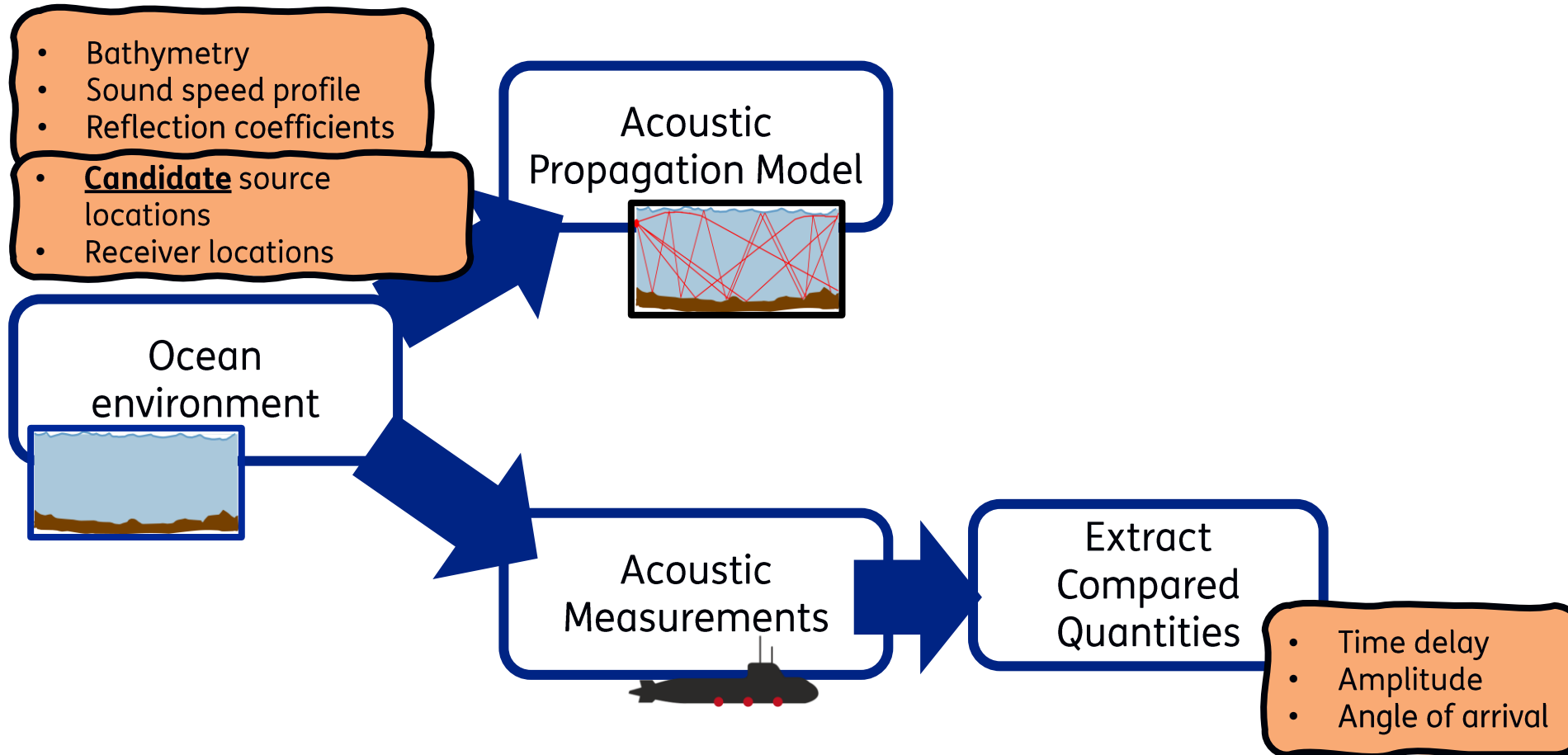
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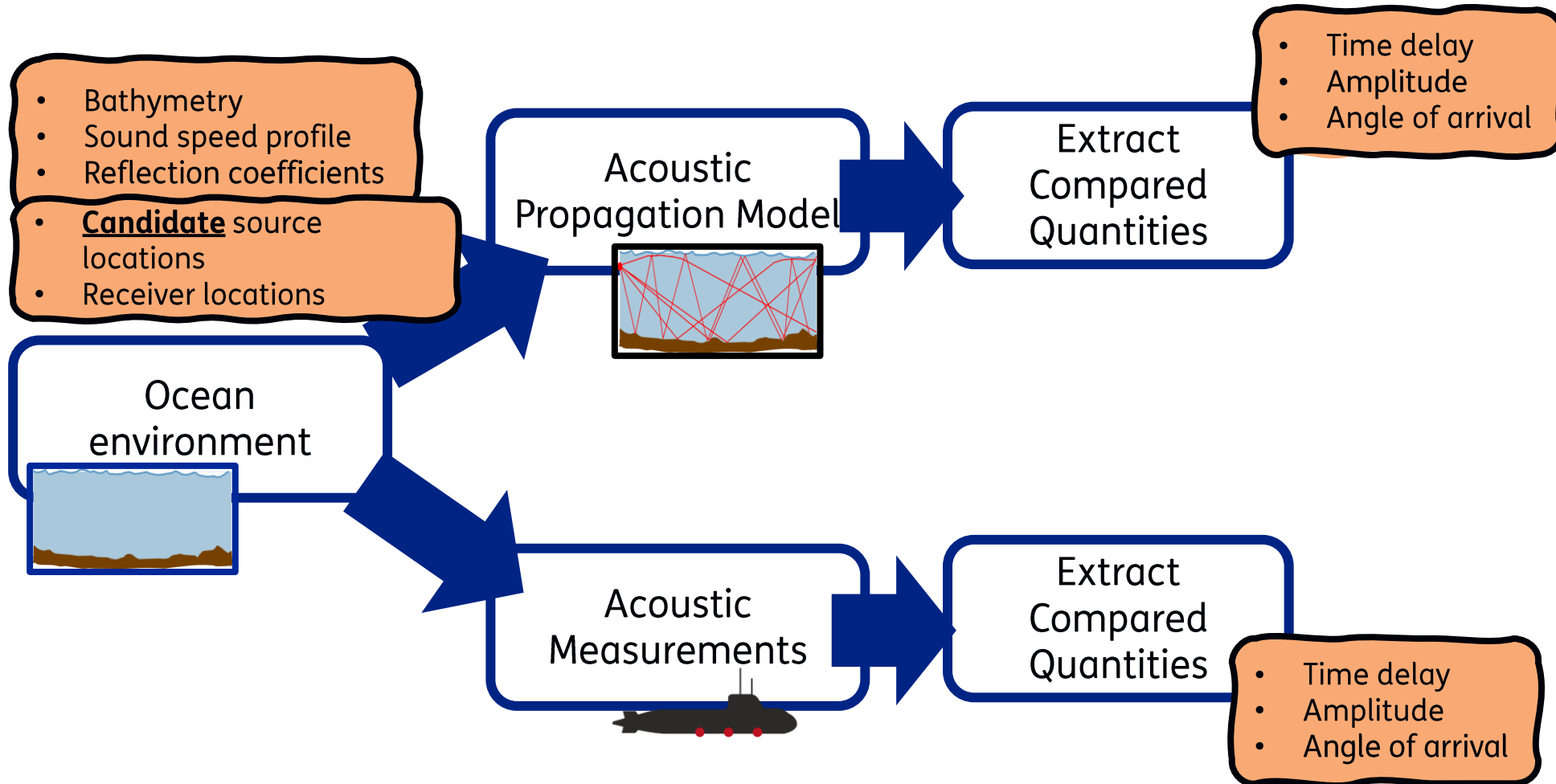
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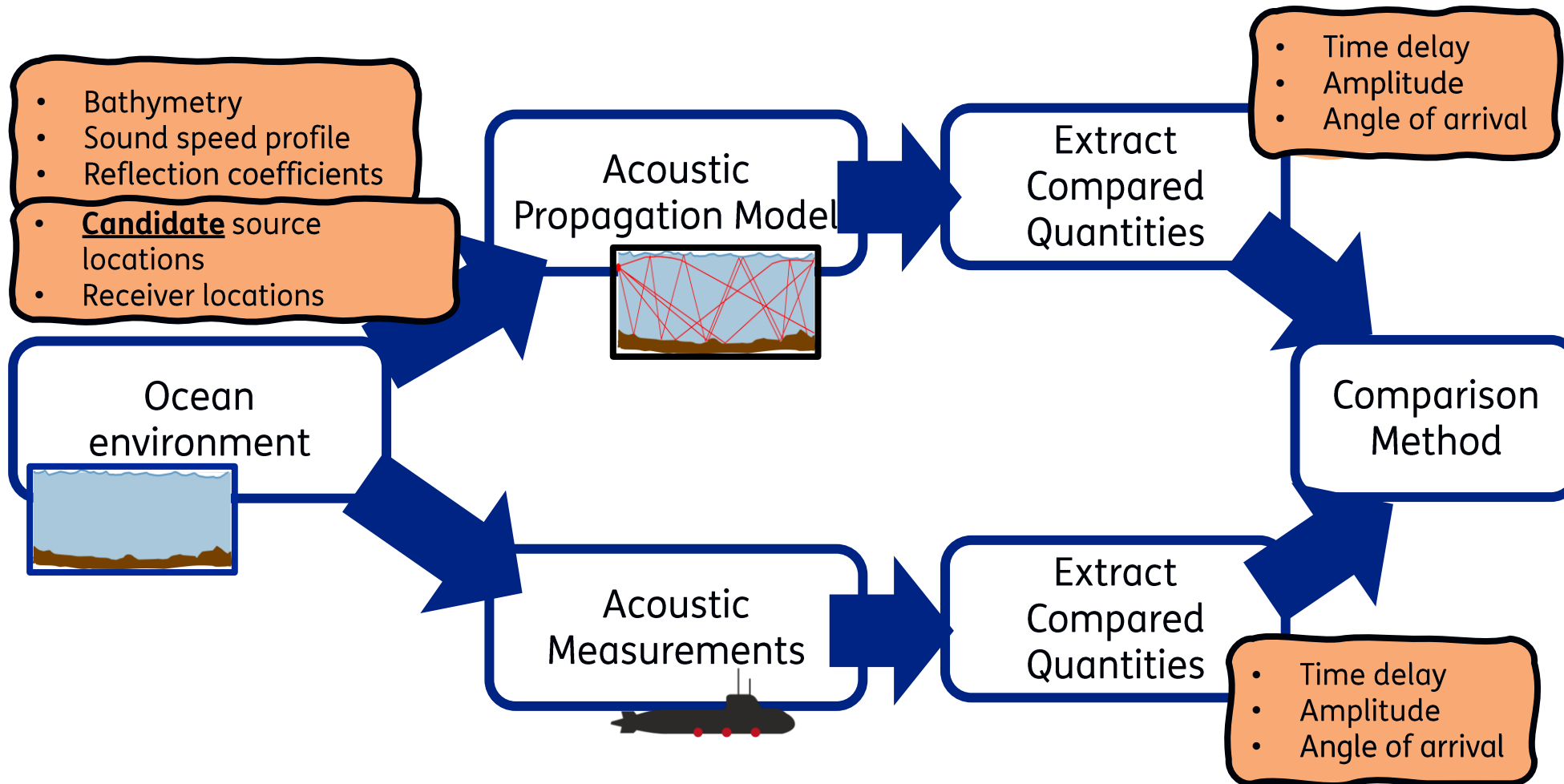
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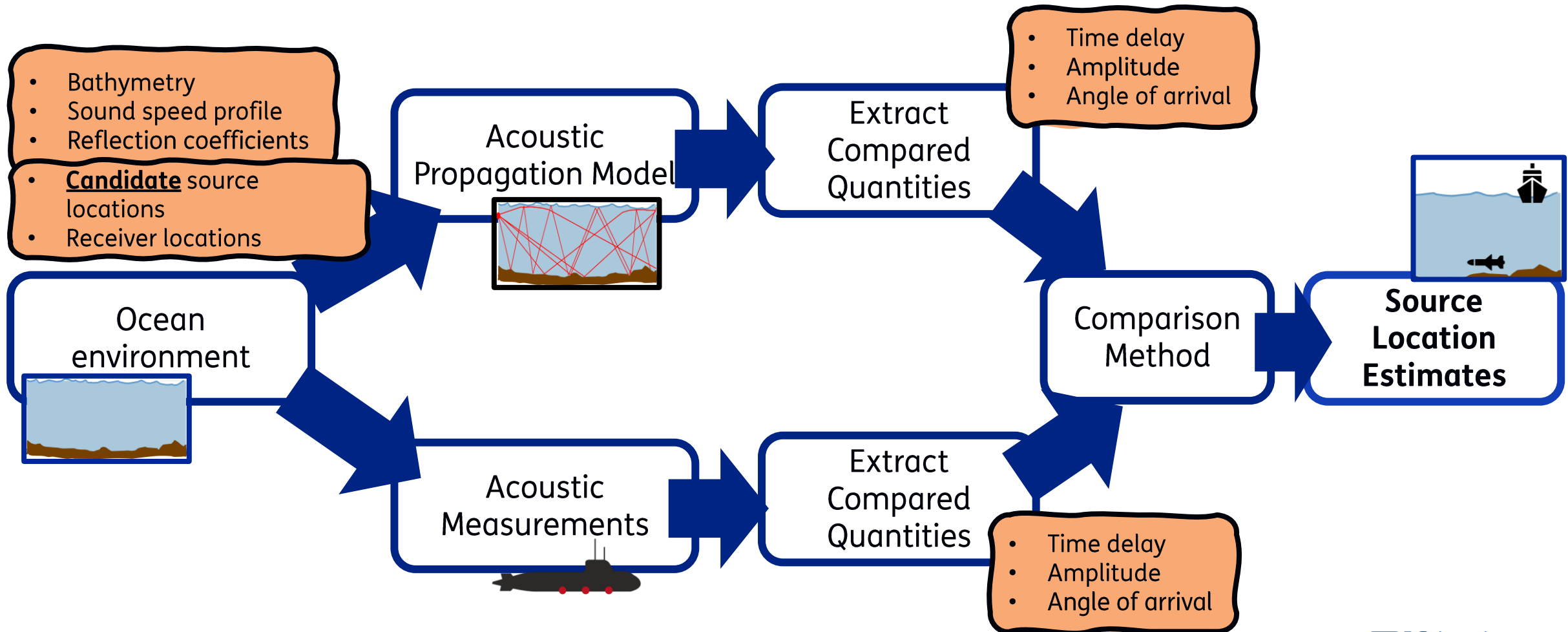
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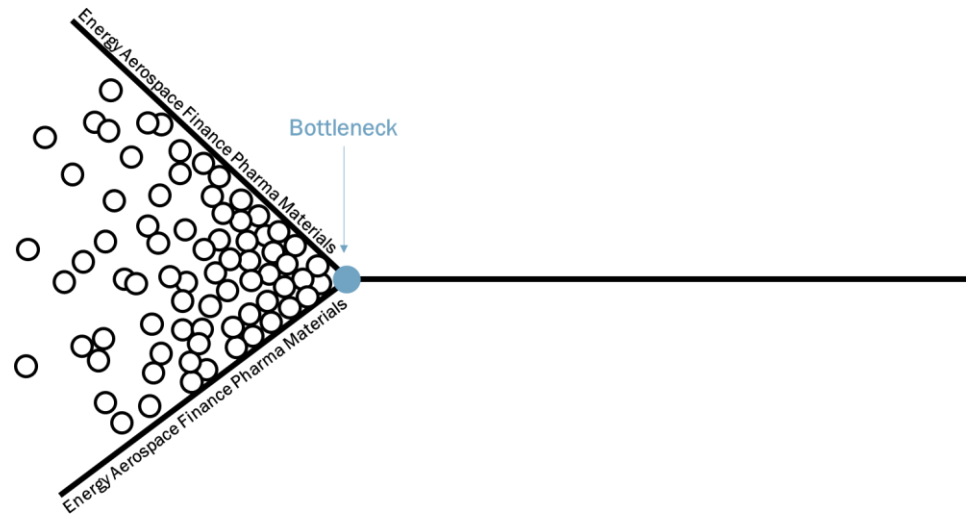
A typical

- Bathymetry
- Sound speed
- Reflection coefficient
- **Candidate** locations
- Receiver locations

Ideally these calculations are performed on **real-time** data on board on a submarine

Applications are limited by the available computational power.

Ocean environment

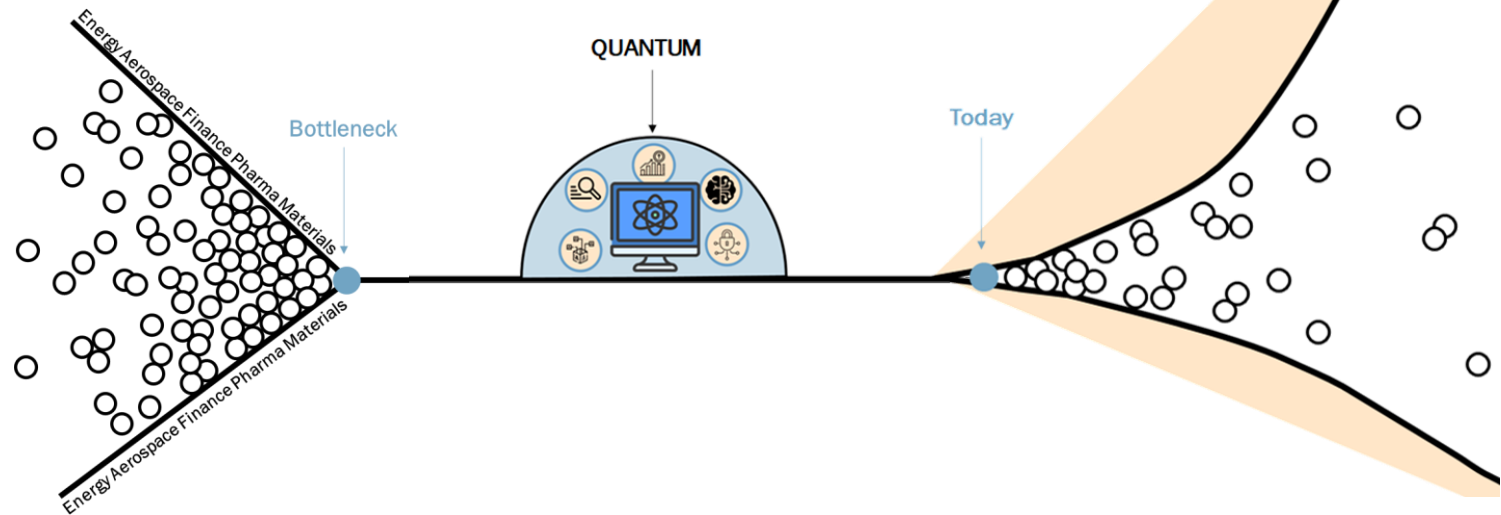


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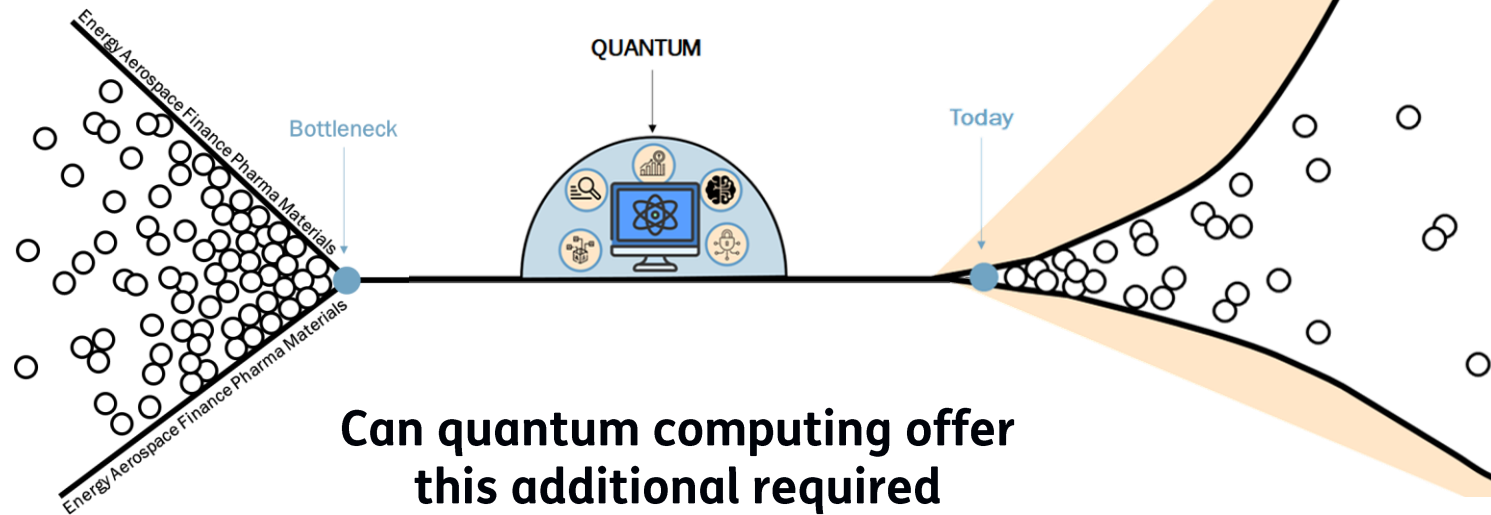
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Can quantum computing offer this additional required computational power?

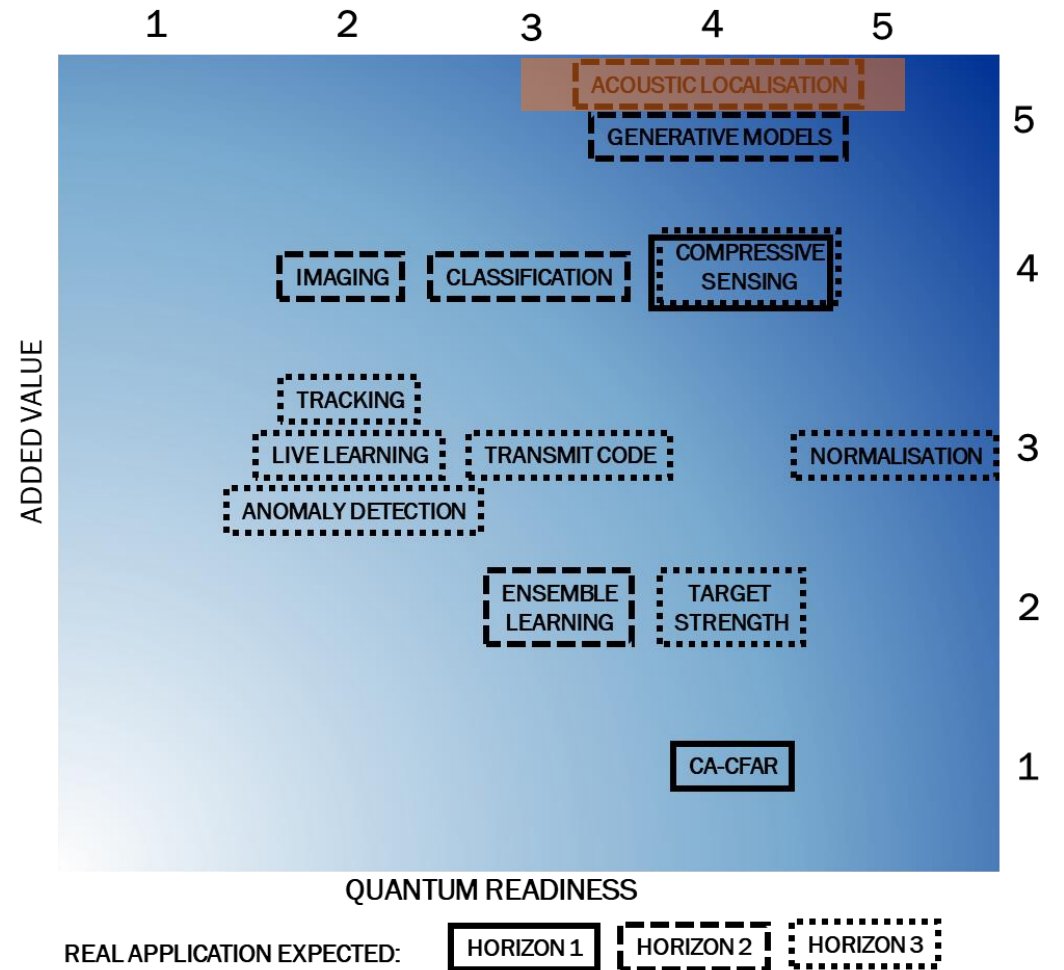
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Potential applications Quantum computing

Quantum computing for radar and sonar information processing

Tariq H. Bontekoe et al., SPIE, 2022,
DOI: [10.1117/12.2618281](https://doi.org/10.1117/12.2618281)



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1. Quantum Readiness – Scale: 1-5

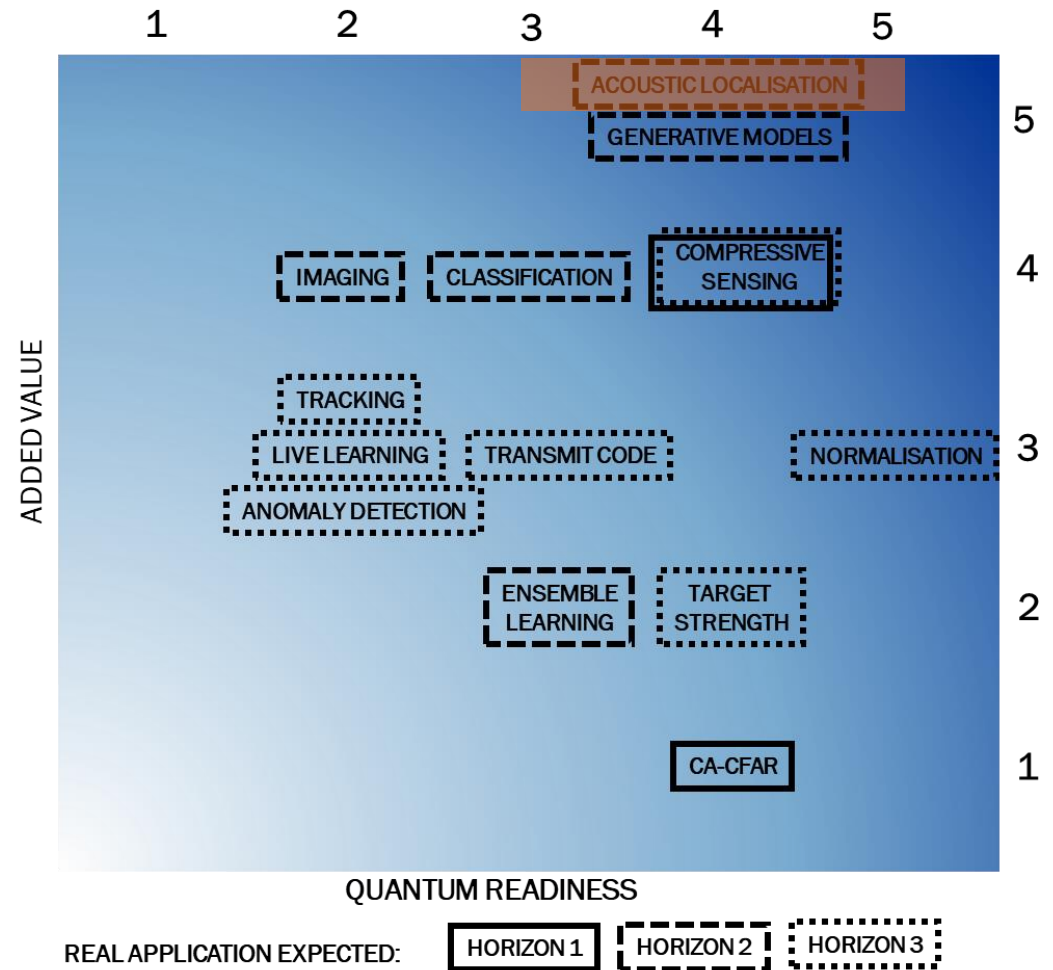
- To what extent is the problem suitable for obtaining a quantum advantage?

2. Added Value – Scale: 1-5

- What is the added value for the defence community to solve the problem faster, better or more effective?

3. Horizon – Scale: 1-3

- When do we expect to run a real sized problem on quantum hardware?



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Various quantum computing paradigms



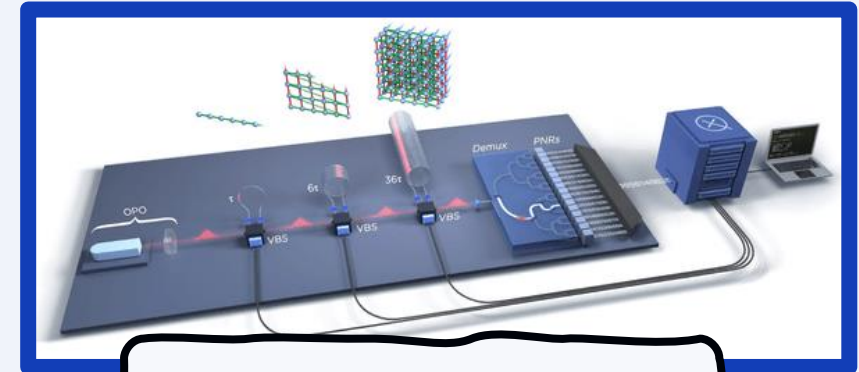
Gate-based quantum computers

QuTech, IBM, Microsoft,
Google, Amazon



Annealing-based quantum computers

D-Wave



Photonic quantum computers

Xanadu, Quix

Various quantum technologies



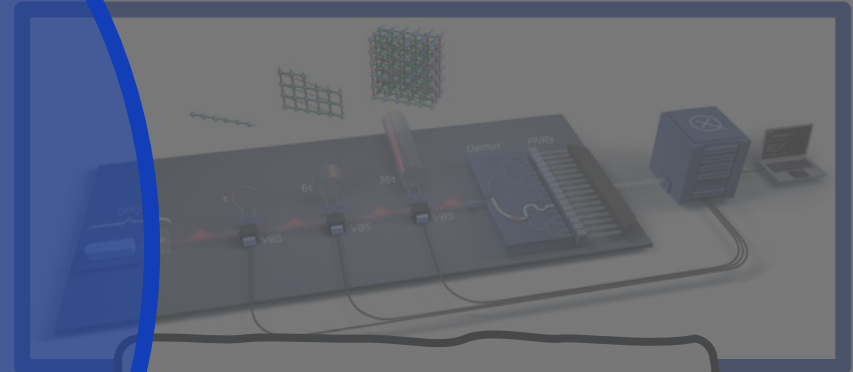
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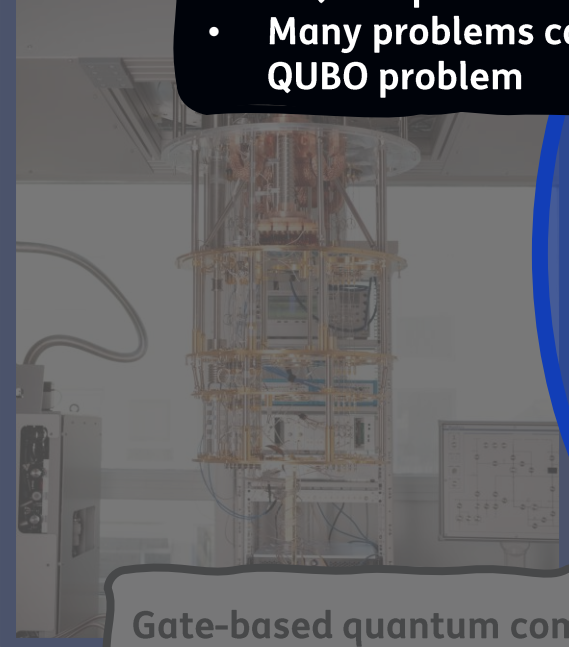
Solve specific type of optimisation problem:

QUBO

Quadratic Unconstrained Binary Optimisation

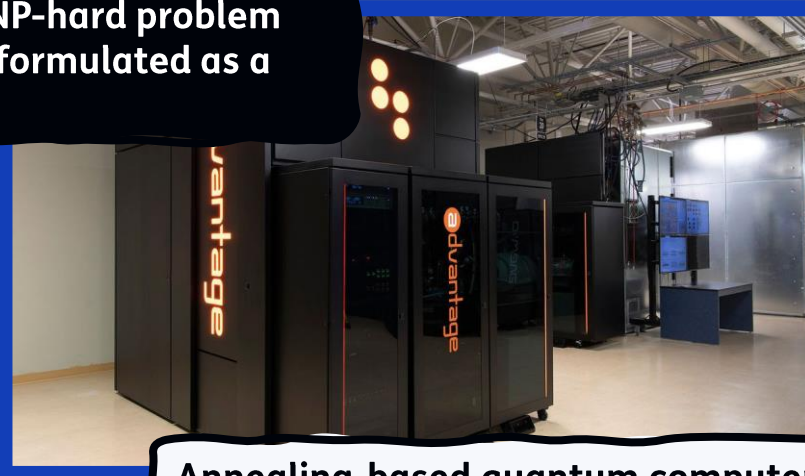
$$\min x^T Q x, \quad x \in \{0,1\}^n, Q \in \mathbb{R}^{n \times n}$$

- A QUBO problem is an NP-hard problem
- Many problems can be formulated as a QUBO problem



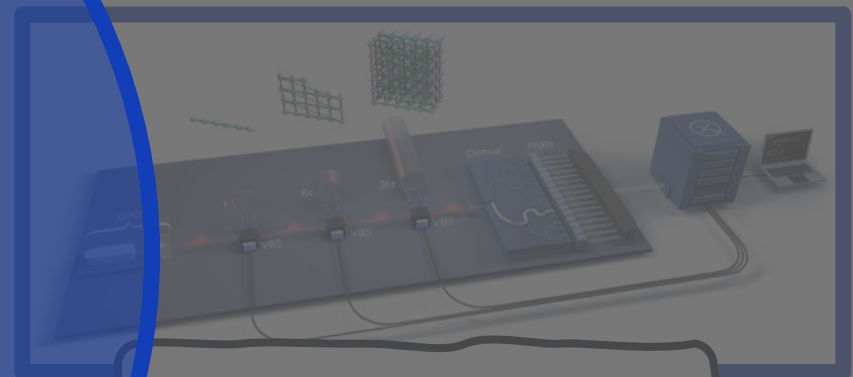
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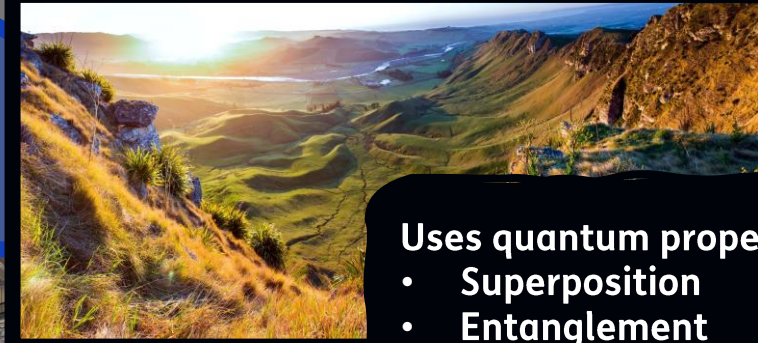
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Encode solution of QUBO as lowest energy state



- Uses quantum properties such as:
- Superposition
 - Entanglement
 - Quantum Tunnelling



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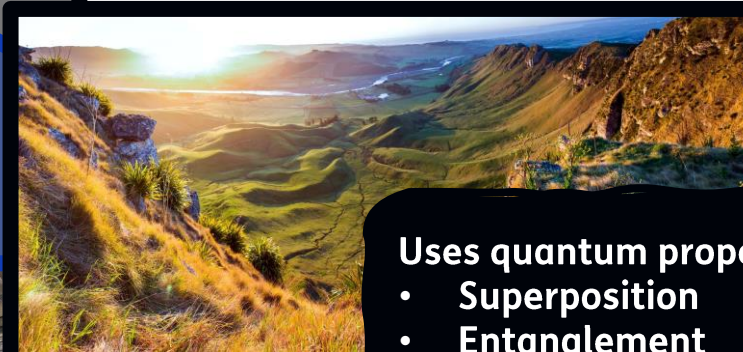
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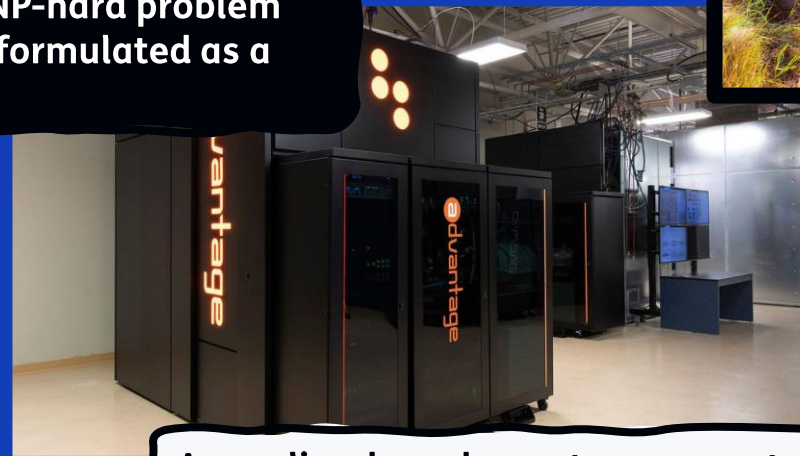
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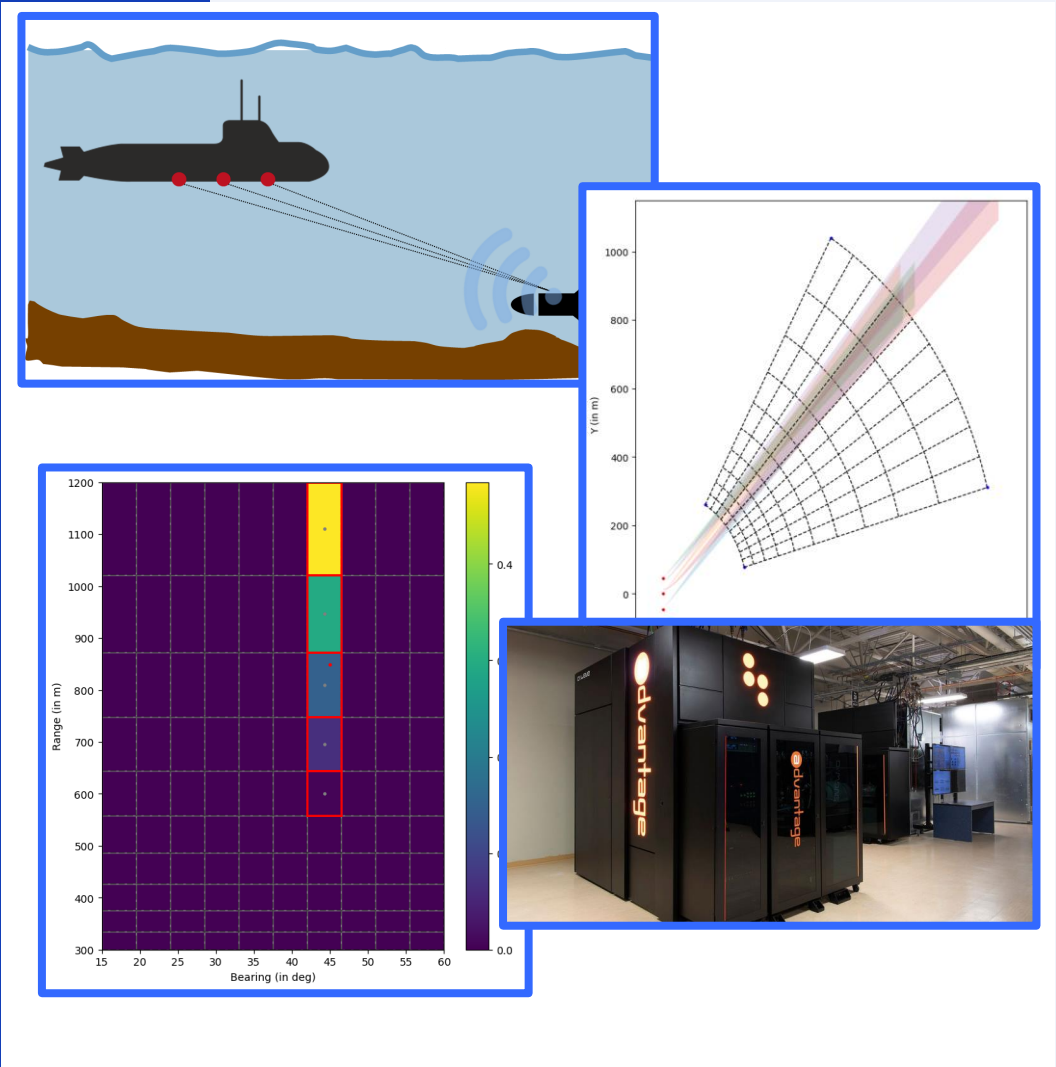
Can be used to efficiently draw samples from a Boltzmann distribution.

Problem modelling

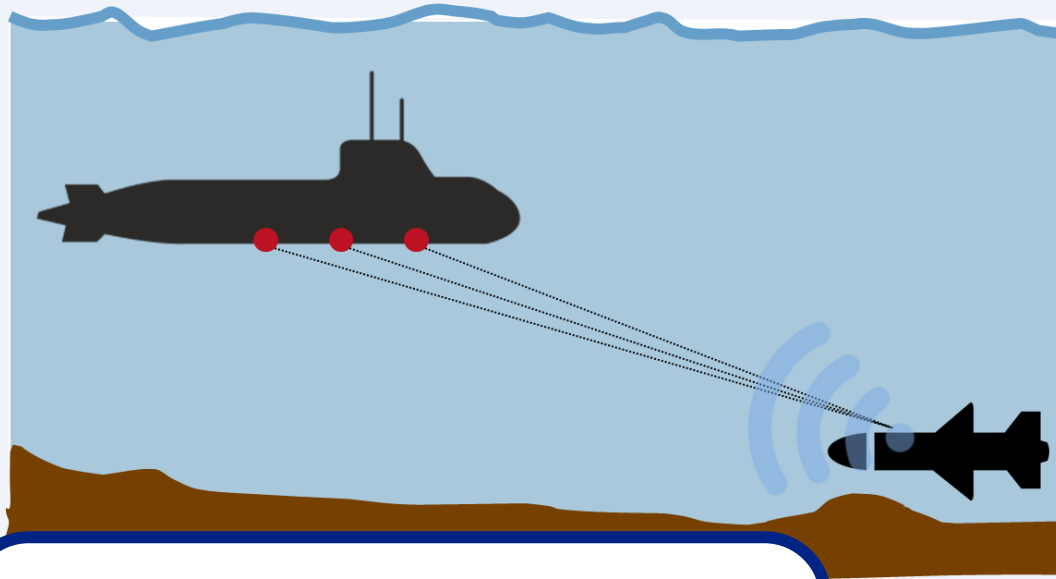
Remodel a **multi-sensor horizontal localisation problem** to a problem that can be solved using a quantum annealer.

Supervised machine learning approach:

- Training the model can be done offline.
- Potentially, enable real-time accurate target estimations onboard once model is trained.
- *Limited size due to available number of qubits and binary variables.*

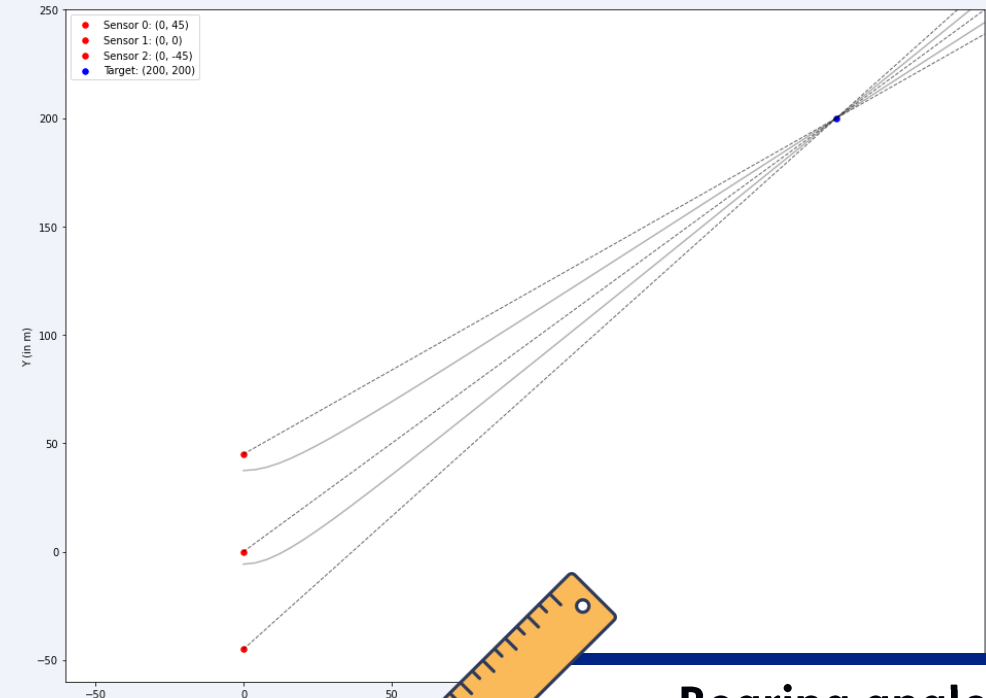


Simplifying assumptions



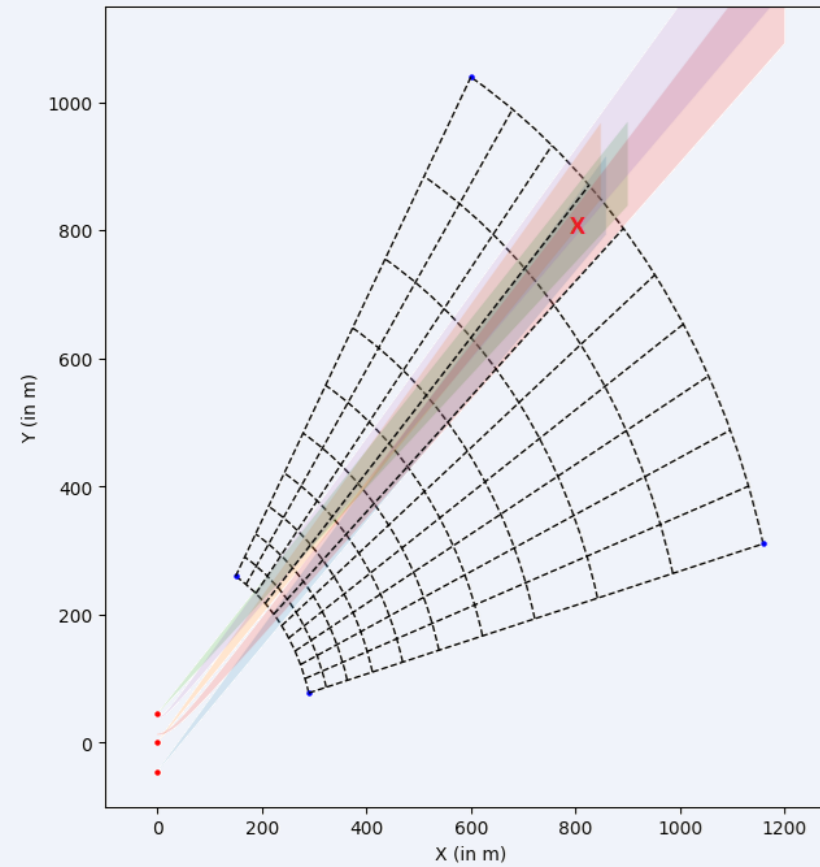
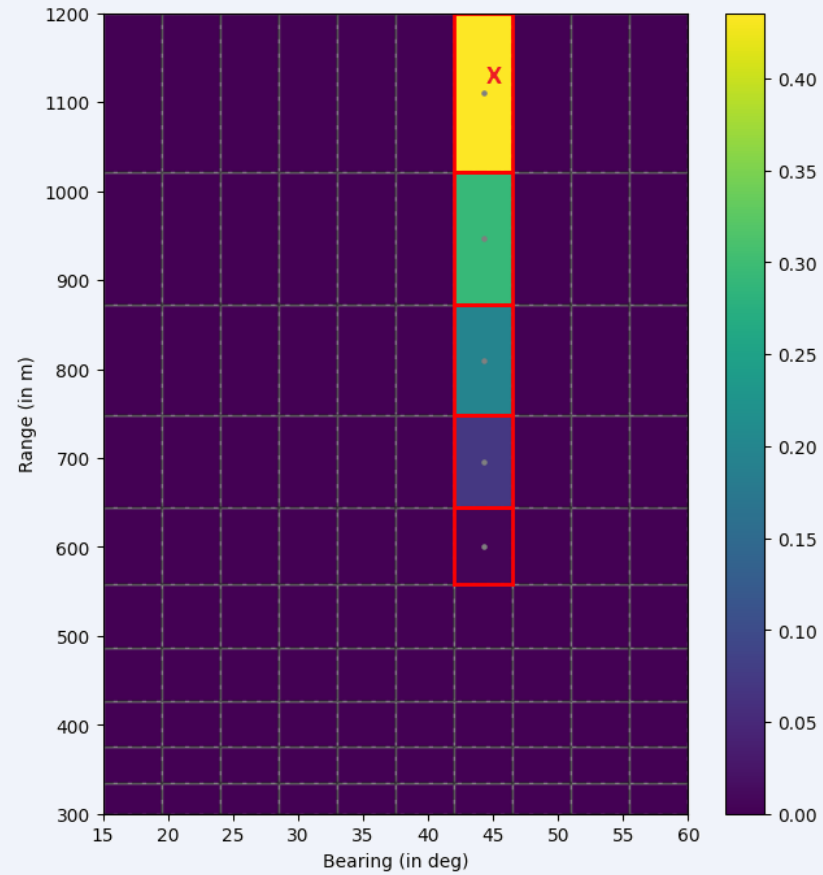
Assumptions:

- 3 sensors on submarine
- Sound propagates **linearly** with **constant velocity**



- 
- Bearing angle 
 - Time difference of arrival (TDOA) 

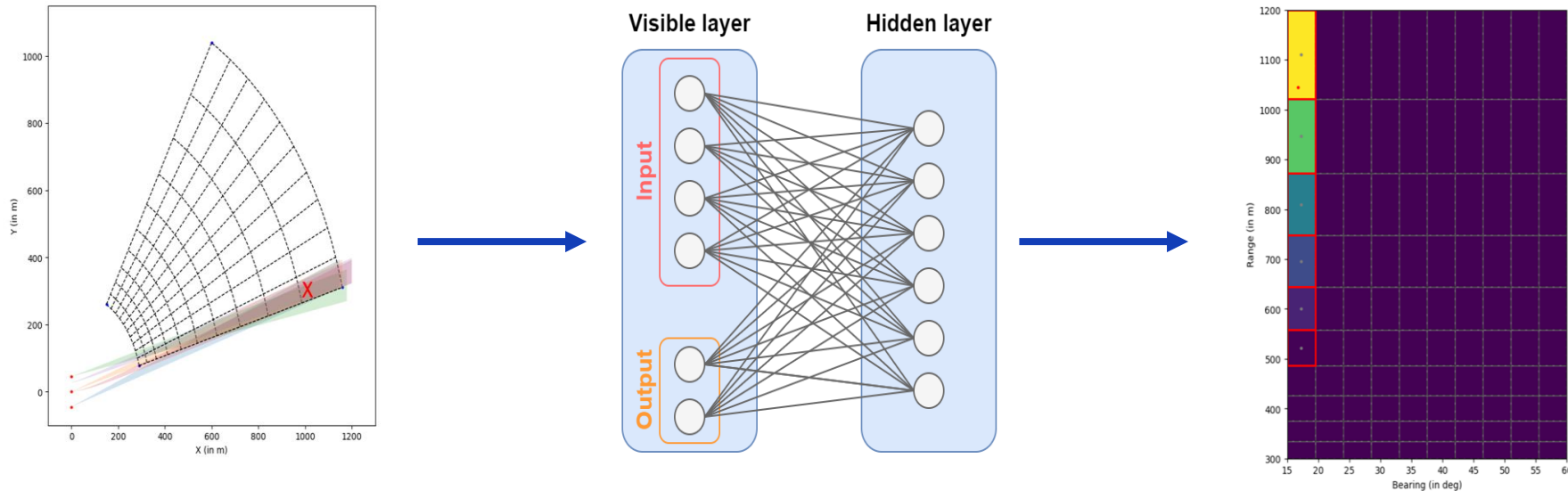
Discretisation of the problem space



Restricted Boltzmann machine

Restricted Boltzmann machine

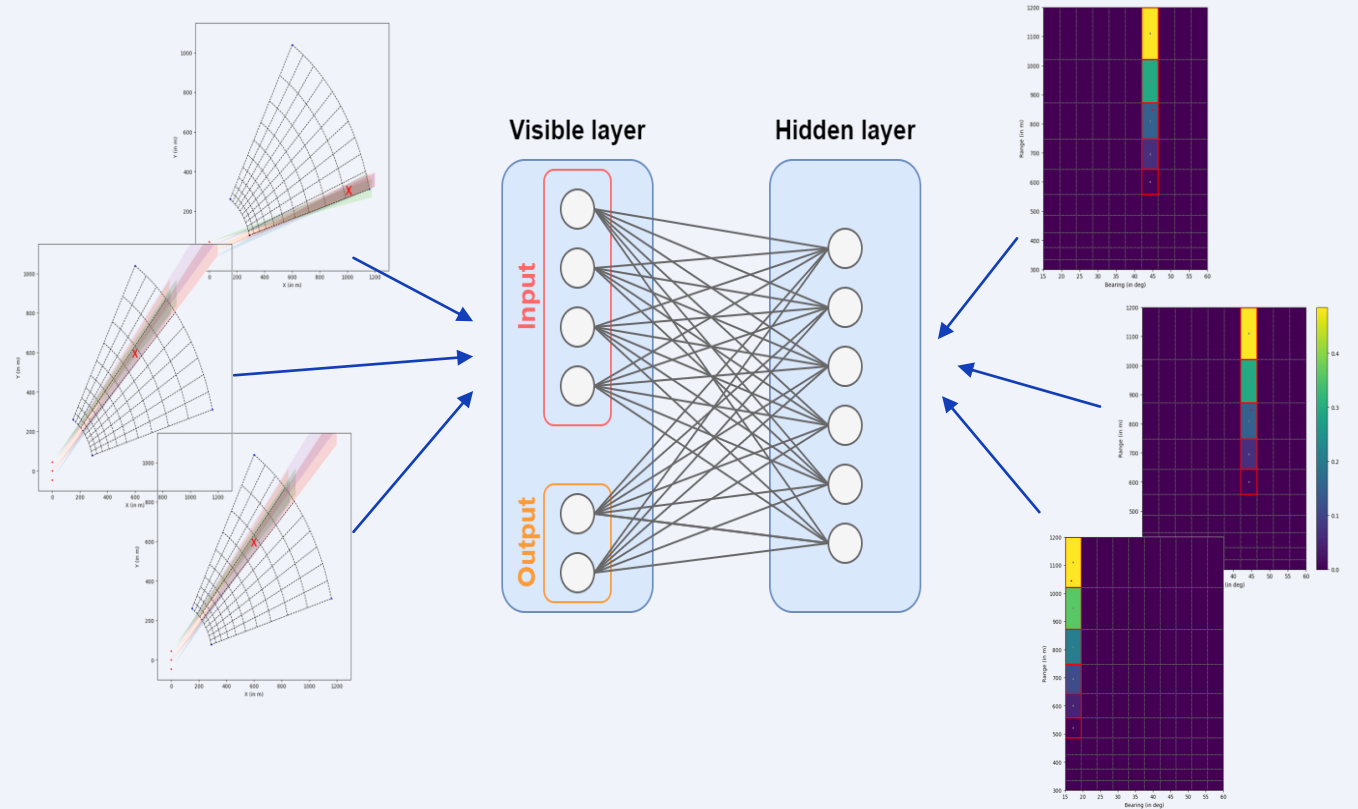
- ‘Neural networks’ used for generative machine learning (supervised learning)
- Offload computation from online procedure to offline procedure



Goal: learn probability distribution over set of inputs

Training the restricted Boltzmann machine

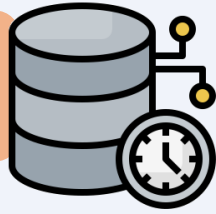
1. Show many inputs + output distribution combinations to the RBM
2. Update weights of the network
3. Hope that the RBM is eventually able to learn to predict output distributions



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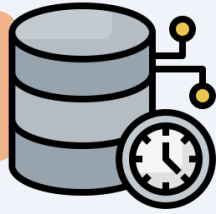
Drawback of restricted Boltzmann machine

Updating weights requires drawing samples from Boltzmann-like distribution which is a computational hard task!

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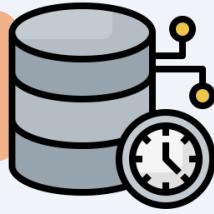
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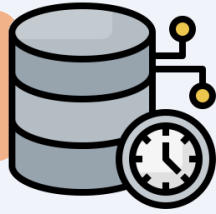
- Utilize the quantum annealer's ability to generate samples from a Boltzmann distribution for training the RBM.
- As a cheaper alternative to study quantum annealing we use simulated annealing.



Training the restricted Boltzmann machine

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3. Hope that the RBM is eventually able to learn to predict output distributions

- Efficient training
- Efficient sampling



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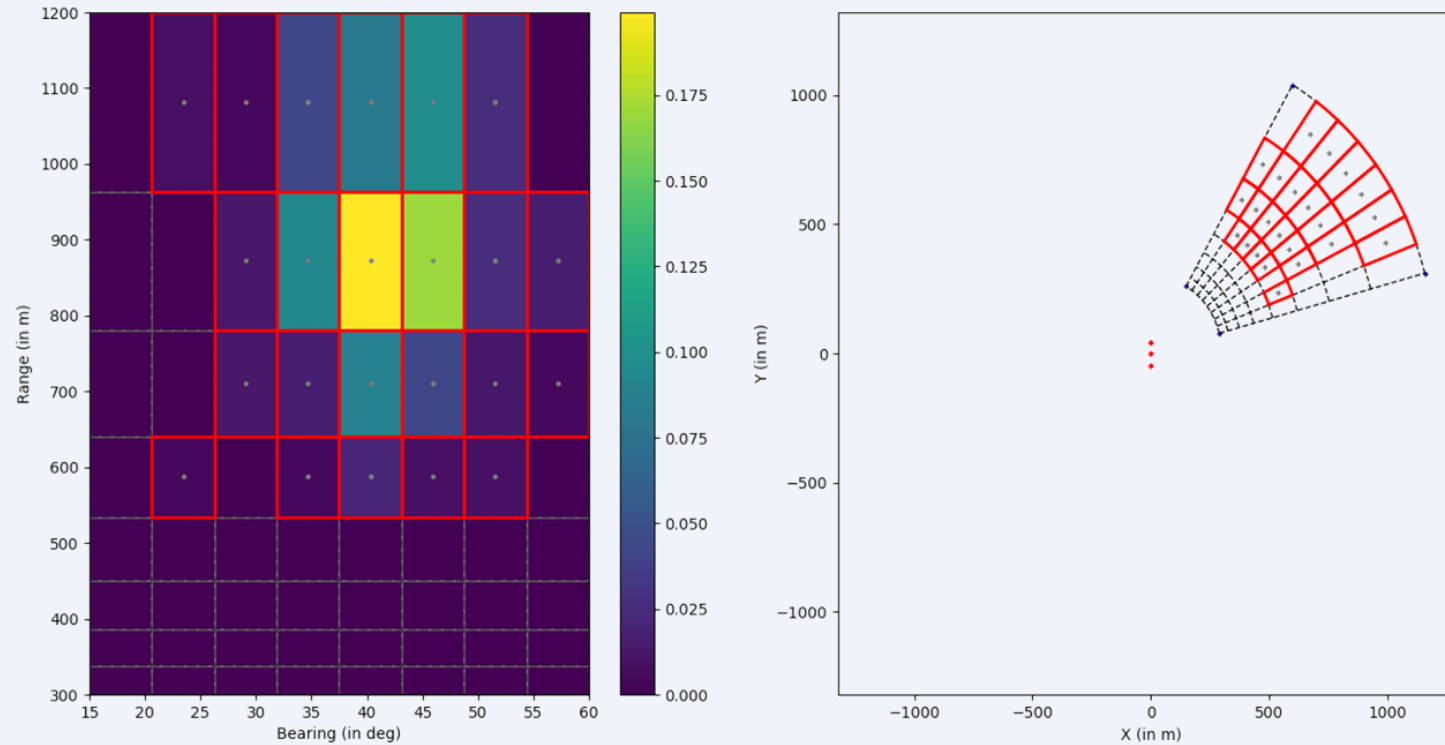
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Example of training

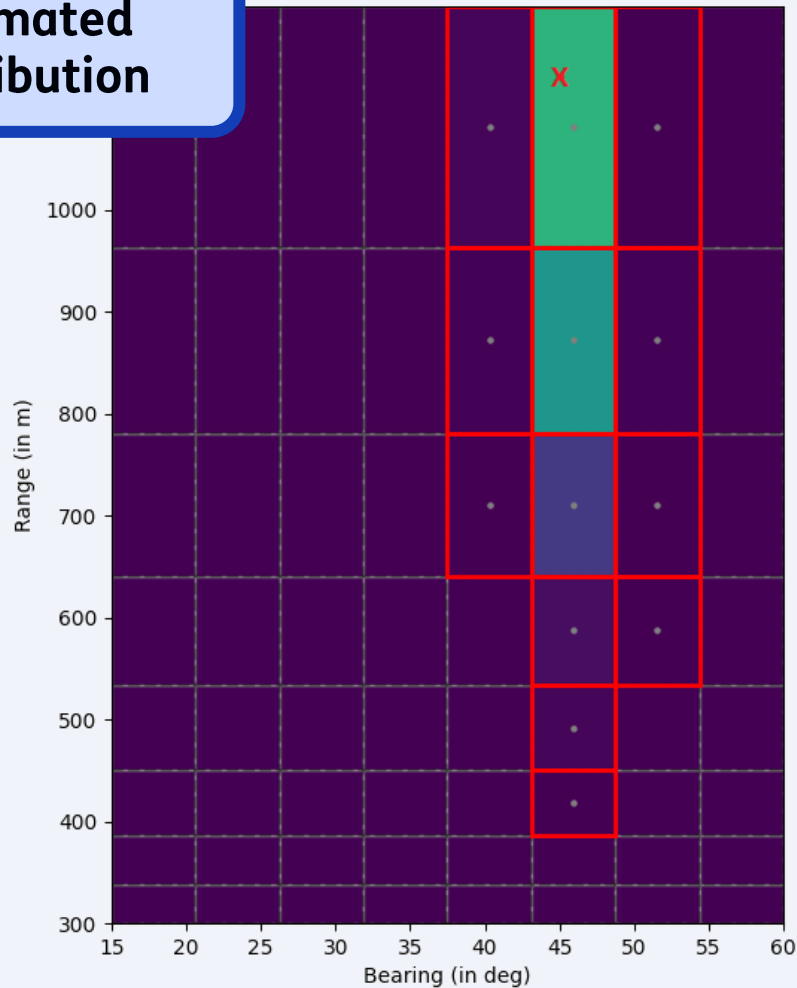
E:5, Model distribution (23.60%) : [9, 9, 9, 10, 10]



Simulated Annealing results

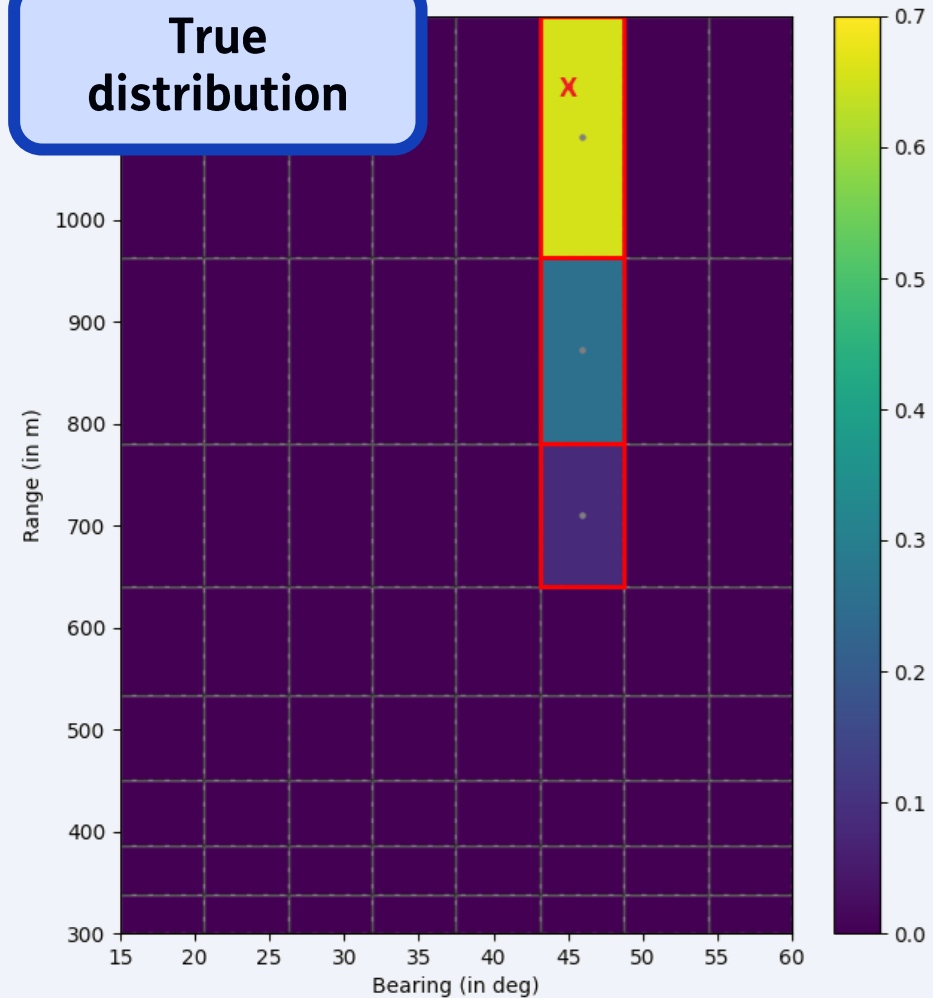
Example: Obtained probability distribution

Estimated
distribution



Simulated Annealing result

True
distribution



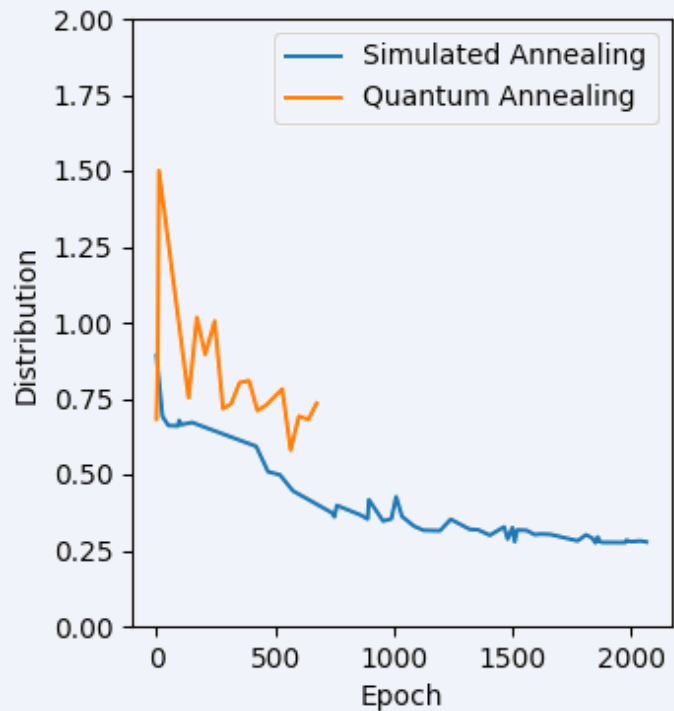
Measures of performances

Distribution

Compares distribution of the environment and the distribution from the *valid* outputs

Range: [0, 2]

Optimal result: 0

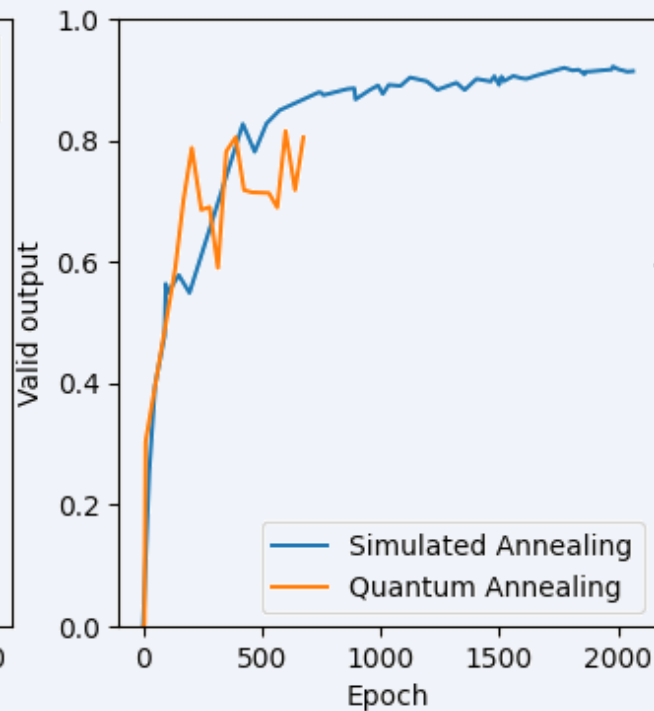


Valid output:

% of output samples with correct output format

Range: [0, 1]

Optimal result: 1

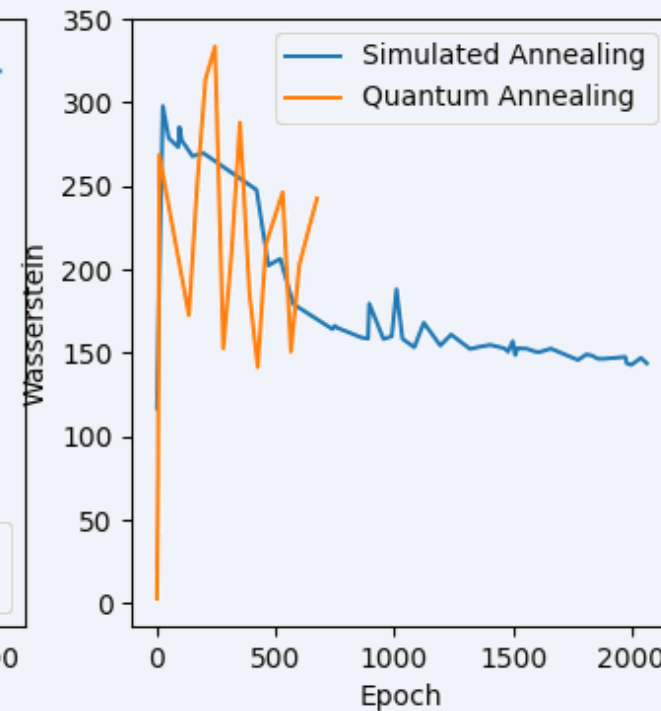


Wasserstein distance

How much work does it cost to transform one distribution into the other distribution

Range: [0, inf]

Optimal result: 0



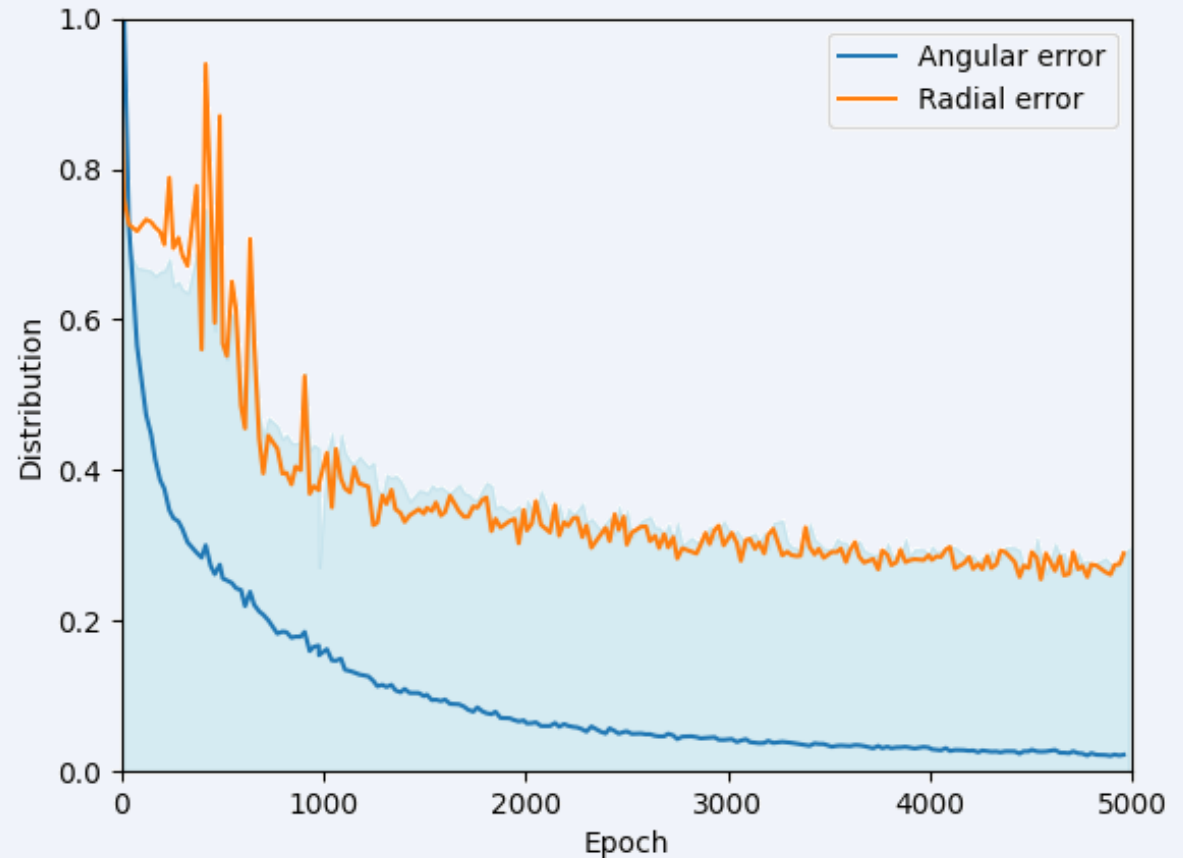
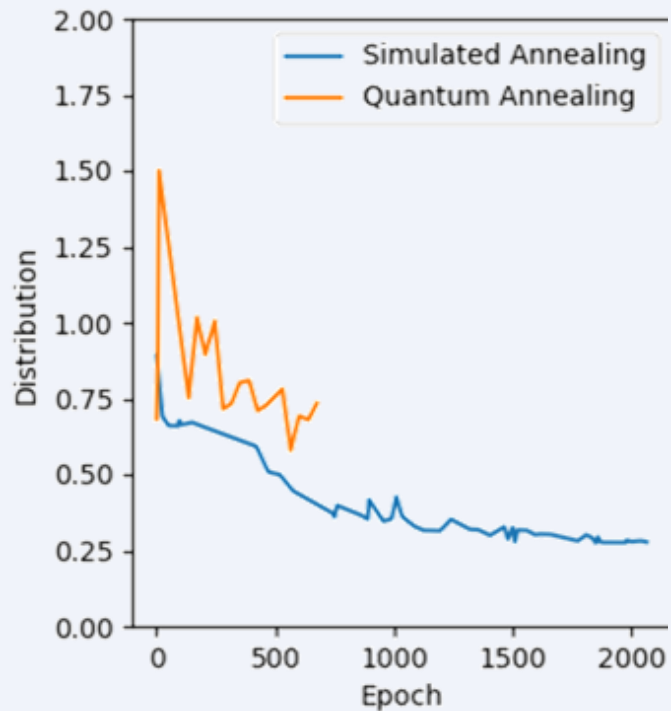
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Simulated Annealing result

Conclusions

Benefits RBM approach:

- Training of the model can be done offline
- Sampling can be done in real-time onboard
- QA can potentially improve training and sampling.



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Current performance

- RBM is able to learn angular dependency well.
- Challenges remain in the radial dependence.
A common problem in acoustic localisation.
- Current hardware size restrict us to small toy problems.



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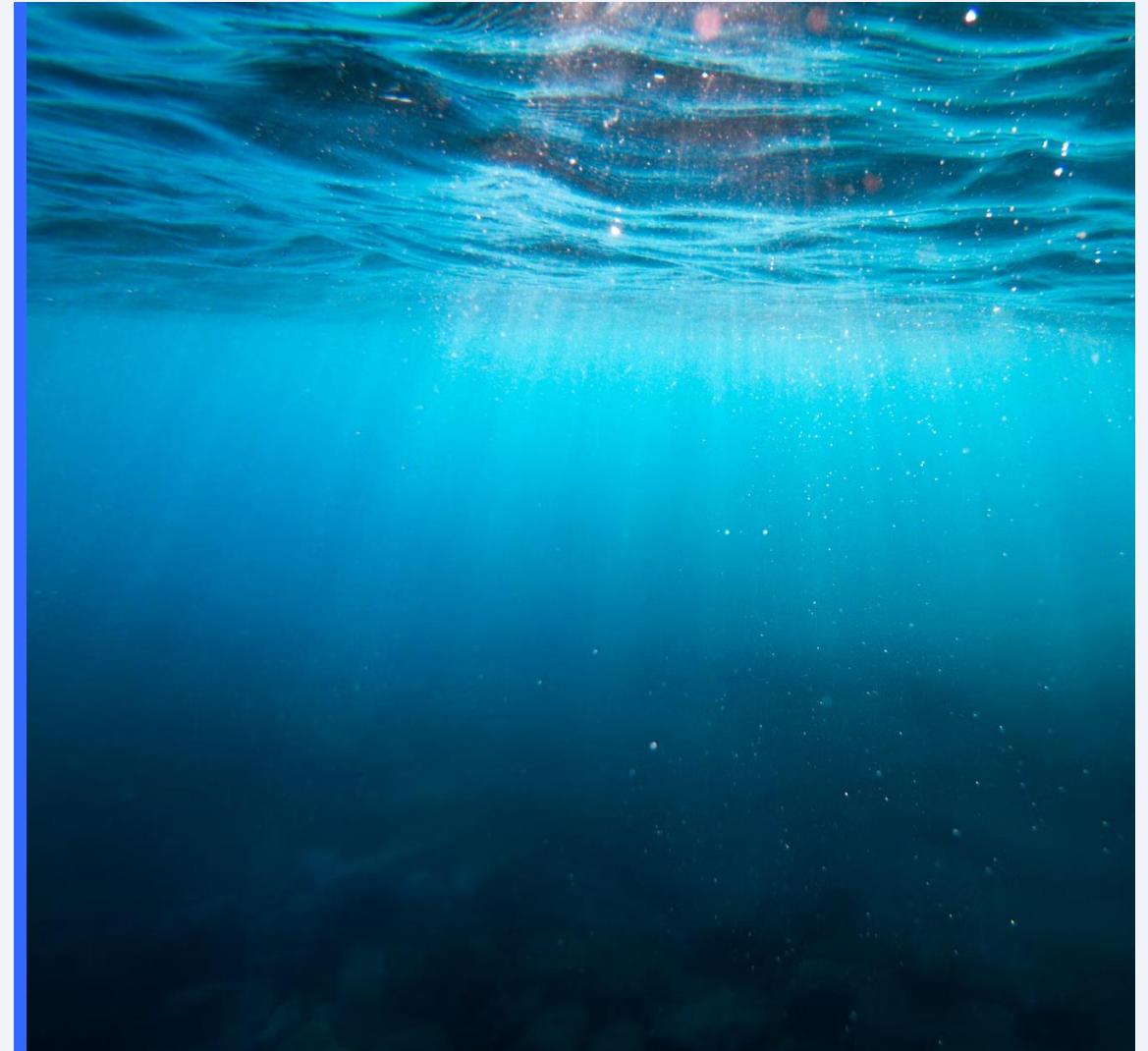
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Next steps

- Comparison with RBM that is trained with conventional techniques.
- Increase complexity of the underwater environment.



Questions & Contact information

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- www.tno.nl/



- www.github.com/TNO-Quantum/

